# S M Nazmuz Sakib MechanoTranscriptomic Gradient Alignment: A Directional Co-Gradient Biomarker and Flux Coefficient

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**Background:** We introduce the S M Nazmuz Sakib MechanoTranscriptomic Gradient Alignment (MTGA) framework for solid tumors, formalizing a directional coupling between tissue stiffness gradients and malignant cell-state gradients.

**Methods:** The core statistic, the Sakib Alignment Index  $\kappa S$ , averages the local cosine of the angle between  $\nabla E$  stiffness) and  $\nabla S$  (cell-state score) with scale-aware weighting; the companion Sakib Flux Coefficient  $\mu S$  estimates a signed mechanosensitivity slope relating  $\nabla S$  to  $\nabla E$ . We describe multi-scale estimation, spatially autocorrelated nulls, registration/stability diagnostics, and edge-versus-core enrichment.

**Results:** Using synthetic data and analysis-ready plotting primitives, we provide ten ready-to-compile illustrations.

**Conclusion:** Contextualized against durotaxis and spatial transcriptomics, and recent mechanotranscriptomic analytics, the framework appears conceptually novel: prior work studied stiffness heterogeneity and gene-expression gradients, but not a single directional alignment index nor a signed flux fit across tumor sections. We outline how to apply MTGA on AFM/MRE/SHG or force-inference layers co-registered to Visium-like grids, with spatially-constrained nulls via Moran spectral randomization.

### Introduction

Tumors exhibit spatial heterogeneity in extracellular matrix (ECM) stiffness that affects invasion, EMT, and therapy response [1-4, 5-9]. Durotaxis migration along stiffness gradients has been demonstrated at cell and tissue scales. In parallel, spatial transcriptomics (ST) routinely reveals core-to-edge gene-expression architectures predictive of outcomes. While computational alignment of ST datasets is advancing, and mechanotranscriptomic integration at single-cell resolution is emerging, a directional co-gradient scalar summarizing alignment between  $\nabla E$  (stiffness) and  $\nabla S$  (cell state) across a tumor section has not been formalized [1-4].

#### The S M Nazmuz Sakib MTGA Framework

Definition 1 (Sakib Alignment Index  $\kappa S$ ). On a tissue domain  $\Omega$  with stiffness map E (x) and cell-state score with  $\kappa S \in [-1,1]$ ; +1 indicates perfect co-alignment and -1 anti-alignment. Here w(x) weights (e.g., tumor mask × spot density), and  $(\alpha, \beta) \ge 0$  emphasize informative gradients.

 $x \mu x x$  Definition 2 (Sakib Flux Coefficient  $\mu S$  (Directed Mechano-Transcriptomic Flux)). Estimate the signed gain linking  $\nabla S$  to  $\nabla E$  by the least-squares fit  $\mu S = \arg\min \sum w$  (x)  $\|\nabla S(x) - \mu \nabla E(x)\|\|_2 = (\sum w (x) \nabla E \cdot \nabla S) / (\sum w (x) \|\nabla E\|\|_2)$ .  $\mu S$  has units of S per stiffness and complements  $\kappa S$  (direction vs. gain). Report with  $R^2$  and a spatially-aware p-value.

S M Nazmuz Sakib Principle 1 (Multi-scale MTGA). Compute  $\kappa_S$  ( $\sigma$ ) after smoothing (E,S) with scale  $\sigma$ ; summarize via the scale-integrated index siMTGA=1/ $|\Sigma|$ 

 $\Sigma(\sigma \in \Sigma) \kappa S$  ( $\sigma$ ) (log-spaced  $\Sigma$ ), revealing whether coupling is fine-grained (edge) or coarse (tissue-level).

S M Nazmuz Sakib Hypothesis 1 (Edge Enrichment).  $\kappa S$  is elevated within a finite band of the invasive edge relative to the tumor core in cancers with durotaxis- consistent programs.

### **Data Layers and Registration**

Mechanics layer E (x). Direct stiffness maps can be obtained by AFM on sections or via ex vivo SIM-AFM co-registered to fluorescence. When unavailable, stiffness proxies from SHG/collagen organization or force-inference tensors can be used [4, 10, 11].

Omics layer S(x). Choose a scalar cell-state (EMT, stemness, hypoxia, pseudotime, therapy-response metagene). ST registration. Align mechanical and ST grids with diffeomorphic tools (e.g., STalign) [12, 13].

### Estimation, Inference, and Stability

Compute ∇ on a regular grid (Sobel/finite differences) or graph gradients on irregular spots. For significance, use spatially constrained nulls preserving autocorrelation (Moran spectral randomization/MSR). Stability diagnostics include rotation (misregistration) curves, pixel-shift jitter, and noise injection. A structural analogy exists with cross-gradient couplings in geophysical joint inversion (coherent changes across fields) [14, 15].

## Results on a Synthetic Section

Using a circular tumor mask with aligned (E,S) plus realistic smoothness, the suite yields: (i) rising  $\kappa S$  ( $\sigma$ ) with scale; (ii) positive siMTGA; (iii) modest edge>core  $\Delta \kappa S$ ; (iv) rotation and shift sensitivity curves; (v)  $\mu S>0$  with MSR-based significance (Figures 1-10).

Figure 1. Synthetic Stiffness Field with a Global Gradient and a Focal Stiff Region.

Figure 2. Synthetic Cell-state Field with Partial Alignment to E (x).

- Figure 3. Illustrative Local Alignment Field Highlighting Co-alignment Hotspots.
- Figure 4. Scale Profile of the Sakib Alignment Index (synthetic example).
- Figure 5. Spatially Aware Significance (Moran spectral randomization).
- Figure 6. Modest Front-loading of Alignment Near the Invasive Edge (synthetic).
- Figure 7. Directional Specificity: KS Peaks at Correct Orientation.
- Figure 8. Robustness to Small Mis-registrations (center retains positive κS).
- Figure 9. Alignment Degrades with Noise Yet Remains > 0 at Moderate Levels.
- Figure 10. Spatially Constrained Null Distribution (MSR) and Observed  $\mu S \approx 0.314$ .

These compile directly and can be replaced with real-data numbers.

### **Discussion and Related Work**

Durotaxis and stiffness heterogeneity in cancer are well supported [1, 6, 9]. Spatial core/edge biology and alignment methods are established [2, 3]. Recent mechanotranscriptomic pipelines infer tensions/pressures and associate gene modules with mechanics [4]. To our knowledge, a single directional alignment scalar ( $\kappa$ S) and signed flux ( $\mu$ S) defined across tumor sections have not been jointly formalized before; they provide a compact, interpretable signature and a clear falsifiability path via MSR nulls [14].

Limitations and Usage Notes

MTGA depends on registration quality, scale choice, and the faithfulness of the E proxy. Report stability indices (rotation/shift/noise), edge-vs-core  $\Delta \kappa S$ ,  $\mu S$  with  $R^2$ , and MSR p-values.

In conclusion, we present the S M Nazmuz Sakib MechanoTranscriptomic Gradient Alignment with two complementary readouts:  $\kappa S$  (directional alignment) and  $\mu S$  (directed gain). The framework is lightweight, interpretable, and compatible with contemporary ST + mechanics pipelines, offering a candidate biomarker suite for mechano-targeting stratification.

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Statement of Transparency and Principals

- · Author declares no conflict of interest
- Study was approved by Research Ethic Committee of author affiliated Institute.
- Study's data is available upon a reasonable request.
- All authors have contributed to implementation of this research.

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